1. Control algorithm for dosing magnesium hydroxide in sewers

1.1 Background

Mg(OH)\(_2\) dosing in sewers prevents sulfide transfer from the liquid to the gas phase by increasing the pH of the sewage. The maximum pH achievable by Mg(OH)\(_2\) dosing is approximately 9.0-9.2. At such pH levels, the percentage of H\(_2\)S in the liquid is less than 1%. Long-term pH elevation to 8.6–9.0 reduces SRB activity by 30%-50%.

Further information can be obtained as follows:

- Effects of Mg(OH)\(_2\) dosing:

1.2 Control Strategy

The fundamentals for magnesium hydroxide dosing control design are discussed, focusing on dosing location and dosing requirements. Additionally the prediction of future flow and the use of a supervisory feedback loop are also discussed.

1.2.1 Dosing Location

The optimal dosing location will largely depend on specific conditions of each system. Some aspects to be taken into consideration include:

- Dosing at the discharge point is simple in terms of control.
- Dosing at the beginning of the pipe minimizes sulfide transfer during the transport (e.g. through air valves), preventing possible odour complaints.
- Dosing at the beginning of the pipe decrease sulfide production and stop methane generation.
- For dosing at the beginning of the pipe, Biological activity (i.e. fermentation) may drive pH down due to the proton production. However such high pH also minimises sewage acidification due to fermentative processes, reducing the amount of magnesium hydroxide to be dosed.
1.2.2 Dosing rate

The Mg(OH)$_2$ dosing rate to achieve a desired set-point at the discharge mainly depends on two factors: the buffer capacity of the sewage and the proton production along the pipe.

1.2.2.1 Buffer capacity

The amount of magnesium hydroxide required to achieve a certain pH is dependent on the actual wastewater pH and the buffer capacity of the sewage. Sewage pH is very dynamic throughout the day, but can be easily monitored on-line using common and inexpensive sensors.

On the contrary, buffer capacity of the wastewater cannot be measured on-line, but needs to be determined by titration as illustrated in Figure 1, which depicts titration curves of sewage at different times of a day.

![Figure 1. Examples of titration curves of sewage at different times of the day.](image)

1.2.2.2 Proton production along the pipe

Protons are produced during the transport of sewage through a pipe, with the subsequent pH decrease. An additional amount of magnesium hydroxide should be dosed to achieve the desired pH at the end of the pipe. The amount of protons produced is estimated by a mathematical model based on HRT and A/V ratio.

$$H^+\text{production} = r_{max} \frac{A}{V} * HRT^n$$

(1)
Where $r_{max}$ is the maximum production rate and $n$ is a parameter of the power function.

### 1.2.3 Future flow prediction

Typical hydraulic retention time (HRT) profiles have been used for the online control. This solution is not ideal because of the high variance in sewers. To achieve a better HRT estimation, sewer future flow prediction is obtained through a multi-step auto-regressive moving average (ARMA) models. The prediction during rain or storm events can be enhanced with exogenous inputs (ARMAX) model.

The ARMA model is composed of both autoregressive (AR) and moving average (MA) models. Equation 2 depicts a general expression to represent an ARMA model:

$$A(z^{-1})y(t) = C(z^{-1})v(t)$$  \hspace{1cm} (2)

Where $z$ is the backshift operator, $z^{-1}y(t) = y(t-1), v(t)$ is zero mean value Gaussian white noise and $y(t)$ is the observed data.

$$A(z) = 1 + a_1z^{-1} + \cdots + a_{na}z^{-na}$$  \hspace{1cm} (3)

$$C(z) = 1 + c_1z^{-1} + \cdots + c_{nc}z^{-nc}$$  \hspace{1cm} (4)

Where $na, nc$ are the order of $A(z^{-1}), C(z^{-1})$.

ARMA model allowed predicting future flow with reasonably good accuracy under different weather conditions (Figure 2). The delay on the prediction under changing conditions, which is accented at longer prediction times.

Further information can be obtained as follows:

- ARMA model for sewer flow prediction:
  - Paper: Real-time Multistep Prediction of Sewer Flow for Online Chemical Dosing Control

### 1.2.4 Feedback Loop

A feedback loop could help adjusting the dosing rate based on the long-term evolution of the controllable variable, i.e. the pH at the discharge point.

#### 1.2.4.1 Feedback signal

The average discharge pH ($pH_{ave}$) can be used to adjust the overall dosing.

$$pH_{ave}(n) = \alpha \cdot pH_n + (1 - \alpha) \cdot pH_{ave}(n - 1)$$  \hspace{1cm} (5)

where $pH_{ave}(n)$ is the weighted average pH of present time, $pH_{ave}(n - 1)$ is the weighted average pH of previous time, $pH_n$ is the present pH, and $\alpha$ is a weighting factor ($0 < \alpha < 1$).
Aiming to diminish the variation of $\text{pH}_{\text{ave}}$ due to the durative variation of pH signal, a much smaller $\alpha$ ($\alpha = 0.00001$) was chosen.

### 1.2.4.2 Control rule

Based on average pH calculation a proportional control rule is employed to adjust Mg(OH)$_2$ dosing rate.

$$ R_{tb} = k \cdot (\text{pH}_{sp} - \text{pH}_{ave}) $$

Where $R_{tb}$ is the control rule, $k$ is a proportion constant that need to be evaluated, pH$_{sp}$ is set point of pH, pH$_{ave}$ is average pH calculated by eq. 5.

### 1.2.5 Control scheme

The control algorithm for the optimised dosing of Mg(OH)$_2$ is composed of a feedforward and a feedback loop. The feedforward loop will predict the amount of Mg(OH)$_2$ required to increase the pH to 9 and the additional dosing to balance proton production. Moreover, the future HRT will be predicted by the ARMA model using the current flow measurements. Additionally, the feedback loop will adjust the dosing based on the overall performance. A scheme of the control algorithm is depicted in Figure 2.

![Control algorithm scheme for Mg(OH)$_2$ dosing.](image)

**Figure 2.** Control algorithm scheme for Mg(OH)$_2$ dosing.

### 1.3 Case studies

Mg(OH)$_2$ dosing in the Queensberry sewage pump station (SA water) in Adelaide, Australia

Further information can be obtained as follows:
- Case studies of Mg(OH)$_2$ dosing in sewers:
  - **Paper:** On-line control of magnesium hydroxide dosing for sulfide mitigation in sewers: Control development and field validation.